

UAA 3 : Asymptotes et limites

Solutions

A. Limites en un réel

2. Définitions

Exercices :

1. Associe chaque graphique à une ou plusieurs des limites ci-après :

(1) $\lim_{x \rightarrow 0^-} f(x) = -\infty$

(3) $\lim_{x \rightarrow 0} f(x) = -\infty$

(5) $\lim_{x \rightarrow 0^+} f(x) = -\infty$

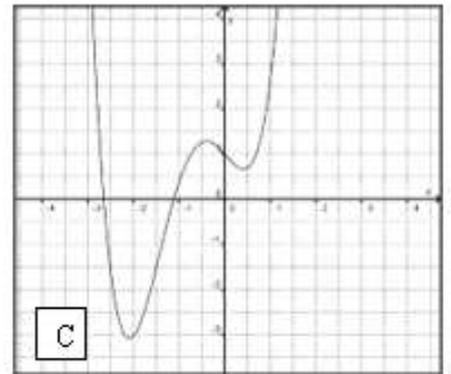
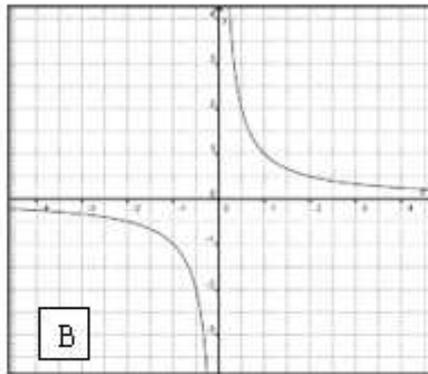
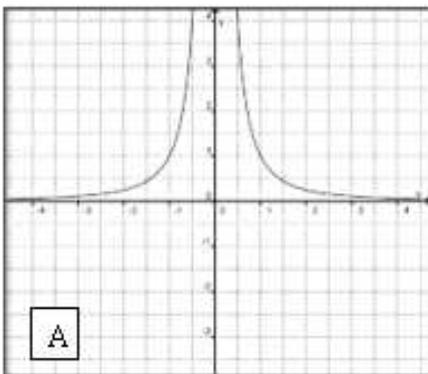
(7) $\lim_{x \rightarrow 0} f(x) = 1$

(2) $\lim_{x \rightarrow 0^-} f(x) = +\infty$

(4) $\lim_{x \rightarrow 0} f(x) = +\infty$

(6) $\lim_{x \rightarrow 0^+} f(x) = +\infty$

(8) $\lim_{x \rightarrow 1} f(x) = 0$



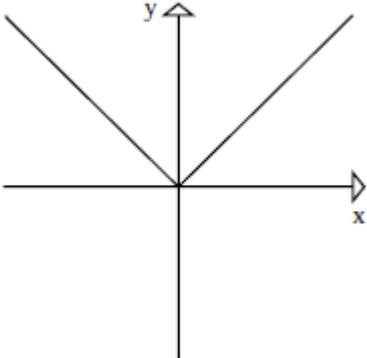
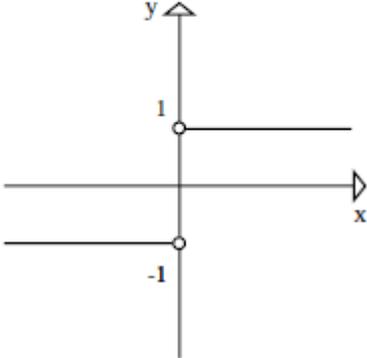
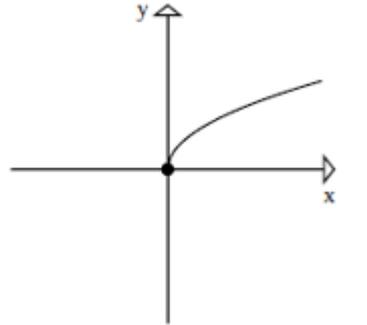
| | | | |
|---------|-----------------------|-----------------------|-----------------------|
| (1) -B | (3) – Aucun graphique | (5) – Aucun graphique | (7) – C |
| (2) - A | (4) - A | (6) – A et B | (8) – Aucun graphique |

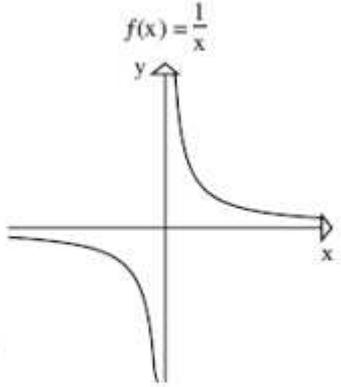
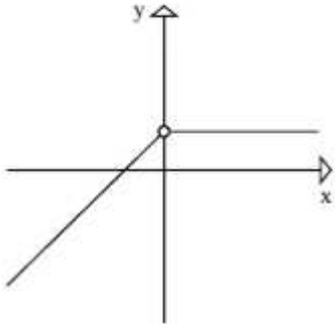
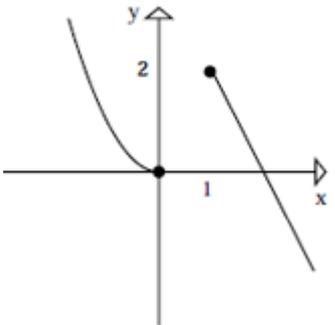
2. Détermine graphiquement chacune des limites :

a. $\lim_{x \rightarrow 0^+} f(x)$

b. $\lim_{x \rightarrow 0^-} f(x)$

c. $\lim_{x \rightarrow 0} f(x)$

| | a. | b. | c. |
|---|----|--------------|--------------|
| $f(x) = \sqrt{x^2}$  | 0 | 0 | 0 |
| $f(x) = \frac{ x }{x}$  | 1 | -1 | N'existe pas |
| $f(x) = \sqrt{x}$  | 0 | N'existe pas | 0 |

| | | | |
|--|--------------|-----------|--------------|
| $f(x) = \frac{1}{x}$  | $+\infty$ | $-\infty$ | N'existe pas |
| $f(x) = \begin{cases} x+1 & x < 0 \\ 1 & x > 0 \end{cases}$  | 1 | 1 | 1 |
| $f(x) = \begin{cases} x^2 & x \leq 0 \\ 4-2x & x \geq 1 \end{cases}$  | N'existe pas | 0 | 0 |